
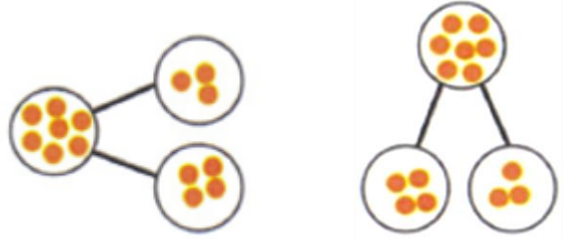
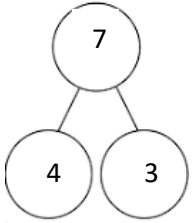
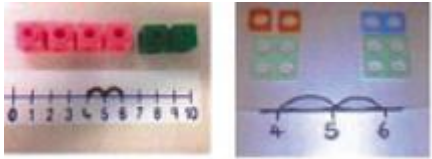
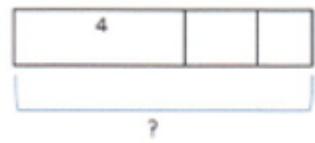
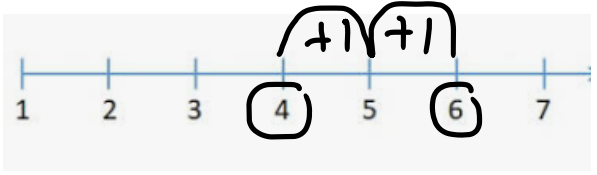

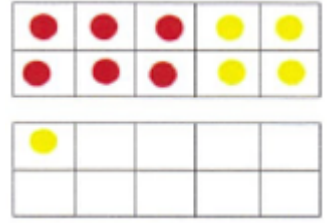




# Maths Calculation Policy

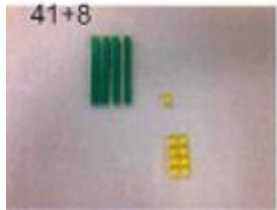
## Addition:

Key language to be used: sum, total, add, parts and wholes, plus, altogether, 'more than', 'is equal to', 'is the same as'.

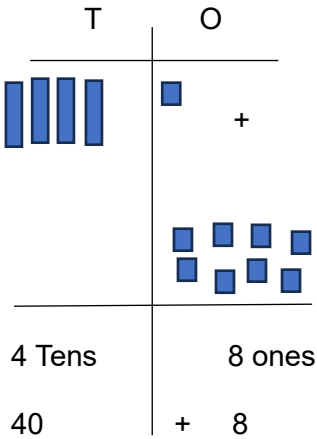
Concrete	Pictorial	Abstract
<p><b>Combining two parts to make a whole</b> (use other resources too e.g. eggs, shells, teddy bears etc.)</p> 	 <p style="text-align: center;">Whole model can face direction.</p>	<p><b>Abstract</b></p> <p><math>4 + 3 = 7</math> (four is a part, 3 is a part and the whole is seven)</p> 
<p><b>Counting on</b> using number lines by using cubes or Numicon.</p> 	<p>A Bar Model encourages children to count on.</p> 	<p>The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What's the total of 2 and 4?</p> 
<p><b>Regrouping</b> to make 10 by using Ten Frames and counters/cubes or using Numicon:</p> <p><math>6 + 5 =</math></p> 	<p>Children to draw the Tens Frame and counters/cubes.</p> <p style="text-align: center;"><math>6 + 5 =</math></p> 	<p>Children to develop and understanding of equality e.g.</p> <p><math>6 + ? = 11</math>    and    <math>5 + ? = 11</math></p> <p><math>6 + 5 = 4 + ?</math></p>

**T + O using Base 10.** (T = tens O= ones)

Continue to develop understanding of partitioning and place value.



Children to represent the concrete using a particular symbol e.g. rectangles for tens and squares for ones.



Children can partition the number to add.

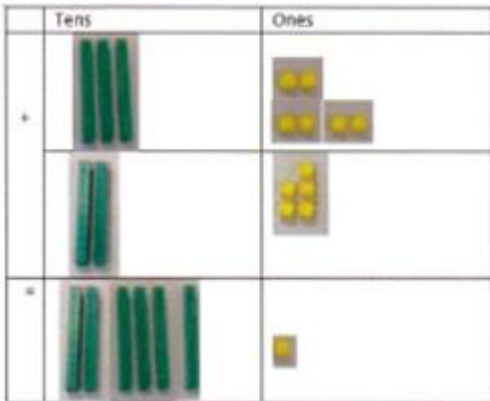
$$40 + 0 =$$

$$1 + 8 =$$

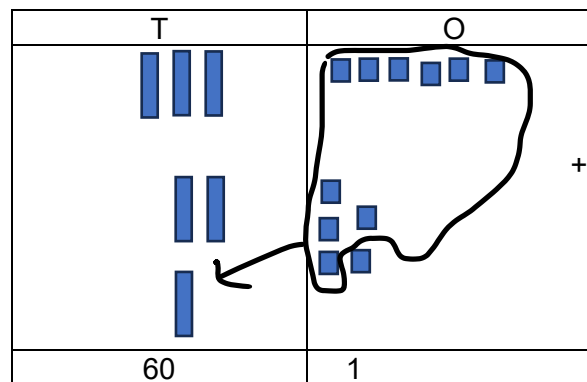
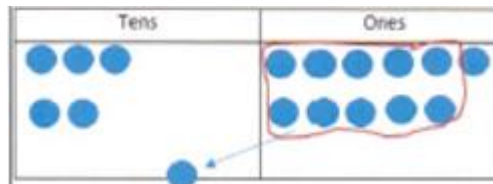
Or Use the Column Method

$$\begin{array}{r} 41 + \\ 8 \\ \hline \\ \hline \end{array}$$

**TO + TO using Base 10.** Continue to develop understanding of partitioning and place value and use this to support addition. Begin with NO exchange.  $36 + 25$



This could be done in more than one way.



$$36 + 25 =$$

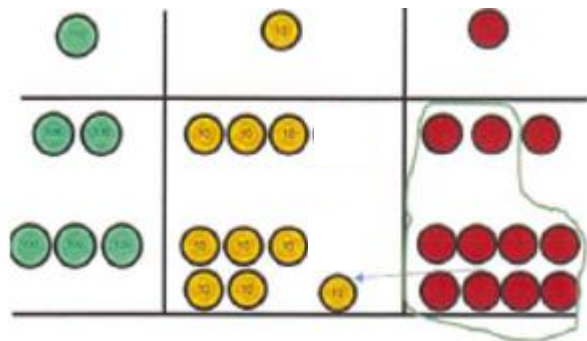
$$30 + 20 = 50$$

$$6 + 5 = 11$$

$$\begin{array}{r} 36 \\ +25 \\ \hline 1 \\ \hline 61 \\ \hline \end{array}$$

**Use of place value counters** to add  
HTO + TO, HTO + HTO etc.  
Again, start without carrying.

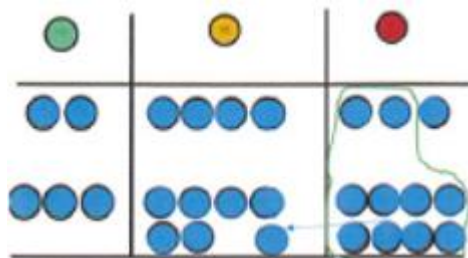
$$233 + 358 =$$



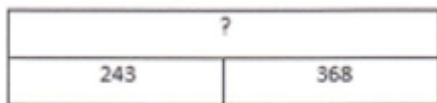
5                      9                      1

There are 11 ones so you take 10 ones and they make 1 ten.

Children to represent the counters e.g. like the image below.



If the children are completing a word problem, draw a bar model to represent what it's asking them to do.



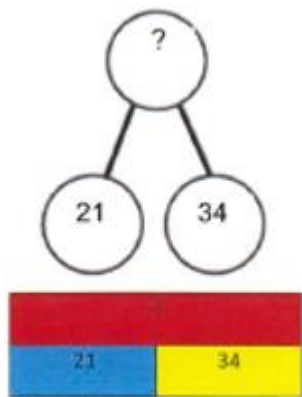
James has 243 sweets, Ben has 368. How many do they have altogether?

Formal Method

$$\begin{array}{r} \text{HTO} \\ 243 \\ 338+ \\ \underline{\phantom{000}} \\ 581 \end{array}$$

We carry the new ten under the ten's column.

### Fluency Variation, different ways to ask children to solve 21 + 34



Sam saved £21 one week and another £34 the next week. How much did he save in total?

$$21 + 34 = 55 \text{ Prove it!}$$

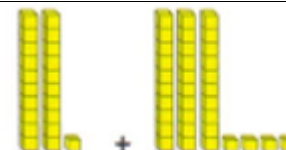
(Reasoning but the children need to be fluent representing this.)

$$\begin{array}{r} 21+ \\ 34 \\ \hline \hline \end{array}$$

$$? = 21 + 34$$

$$21 + 34 =$$

What's the sum of twenty-one and thirty-four?

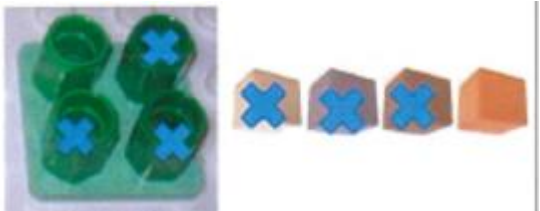


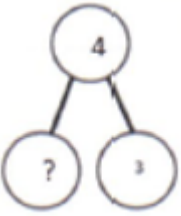

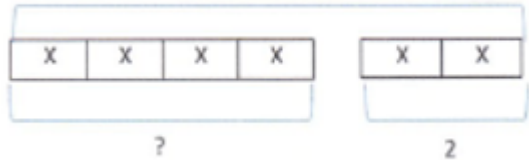
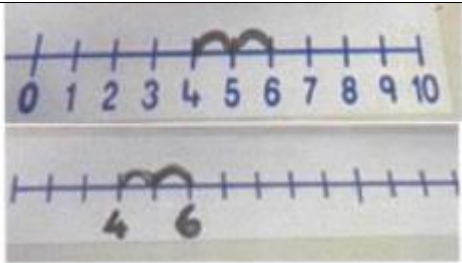
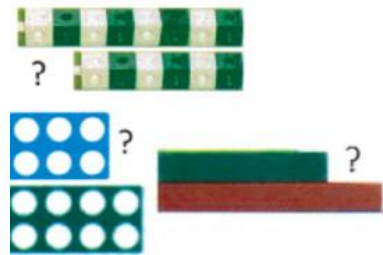
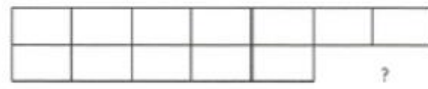


Always use missing digit problems too.



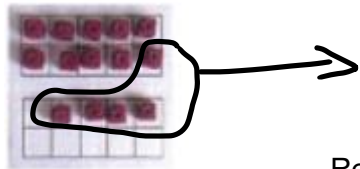
## Subtraction

Key language which should be used: take away, less than, the difference, subtract

Concrete	Pictorial	Abstract
<p><b>Physically taking away and removing objects from a whole</b> (use various objects too) rather than just crossing out.  <math>4 - 3 = 1</math></p> 	<p>Children to draw the concrete resources they are using and crossing out.</p>  <p>Use of the Bar Model:</p> 	<p><math>4 - 3 =</math></p> <p><input style="width: 40px; height: 30px;" type="text"/> = <math>4 - 3</math></p> 
<p><b>Counting back</b> (using number lines or number tracks)</p> 	<p>Children represent what they see pictorially. E.g.</p> <p style="text-align: center;">6</p> 	 <p style="text-align: center;">Children may draw their own number lines</p>
<p><b>Finding the difference</b> (using Numicon or Ten Frames)</p> <p><math>14 - 5 =</math></p> 	<p>Children to draw the cubes/ other concrete objects which they have used.</p> <p>XXXXXXXX          XXXXXX</p> <p>Use of the bar model</p> 	<p>Find the difference between 8 and 6.</p> <p><math>8 - 6</math> the difference is ?</p> <p>Children to also explore why <math>9 - 7 = 8 - 6</math> (difference, of each digit, has changed by 1 so the difference is the same)</p> <p>This will help with numbers like <math>1000 - 567</math>          You would take 1 away from each to make <math>999 - 566</math>.</p>

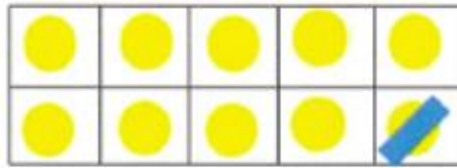
**Making 10** (using Numicon or Tens Frames)

14-5 =



Remove the 5.

Children to present the Ten Frame pictorially.



15 - 5 = 10

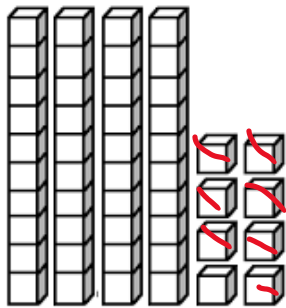
You want children to see related facts e.g.

14 - 5 = 9

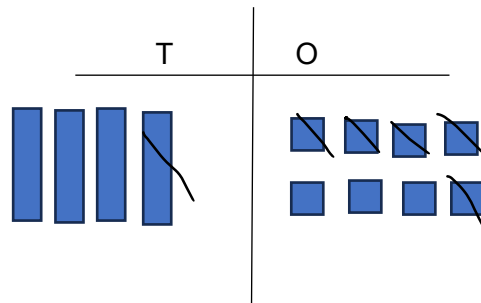
16 - 5 = 11

**Column Method** (using base 10)

48-7 = 41



48 - 15 =



48 - 17 =

48

17-

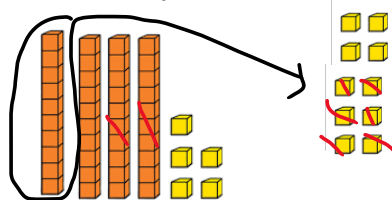
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31

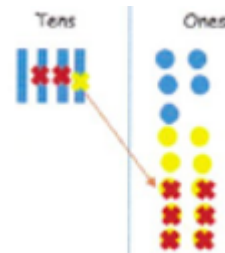
**Column Method** (using Base 10 and having to exchange)

45- 26 = 19

1. Partition the numbers into Tens and ones.
2. Borrow a Ten and make it 10 ones.
3. Then take away the 26.

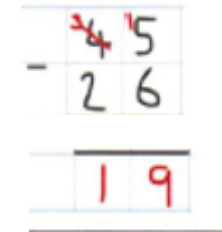


Represent the base 10 pictorially.



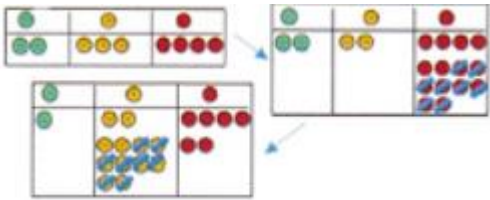
Its crucial that the children understand that when they have exchanged the 10 they still have 45.

45= 30+15



**Column method** (using place value counters)

$$234 - 88 =$$



Once the children have had practise with the concrete, they should be able to apply it to any subtraction.

Like the other pictorial representations, children to represent the counters.

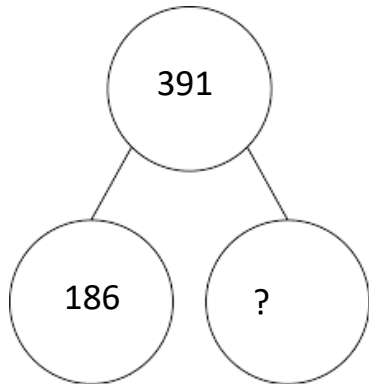
$$\begin{array}{r} \overset{2}{\cancel{2}} \overset{1}{\cancel{3}} 4 \\ - 88 \\ \hline 1 \overset{4}{\cancel{4}} 6 \end{array}$$

<del>200</del>	<del>30</del>	<del>14</del>
100	40	6

1. You can't take 8 from 4 so you have to borrow a ten from the 3 (tens column) and leave 2.  
 $14 - 8 = 6$
2. Then you can't to 2-8 you borrow 100 from the hundreds column.  
 $12 - 8 = 4$
3. Then you look at the 100s column.  
 $100 - 0 = 100.$

### Fluency Variation, different ways to ask children to solve 391-186:

<b>391</b>	
<b>186</b>	<b>?</b>



Raj spent £391, Tim spent £186. How much more did Raj spend?

I had 391 metres to run, after 186 metres I stopped running. How many meters do I have left to run?

$$391 - 186 = 205$$

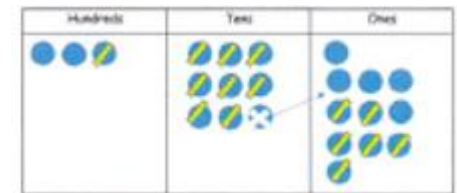
$$\boxed{?} = 391 - 186$$

$$\begin{array}{r} 391 \\ - 186 \\ \hline \end{array}$$

$$205$$


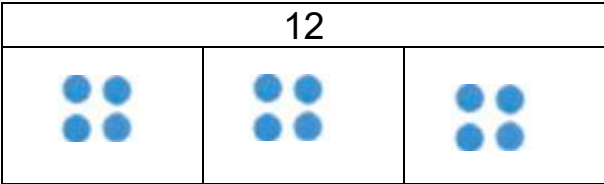
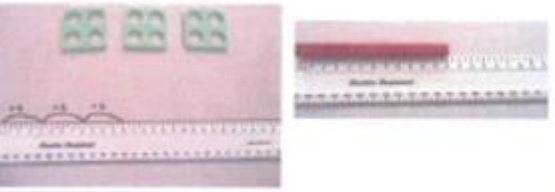

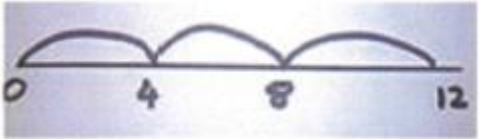

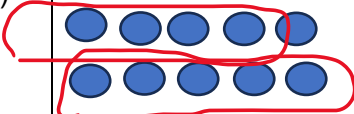
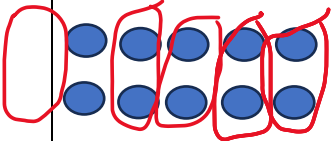
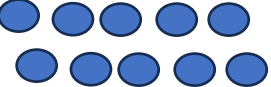
Find the difference between 391 and 186. Subtract 186 from 391. What is 186 less than 391?

What's the calculation?  
What's the answer?



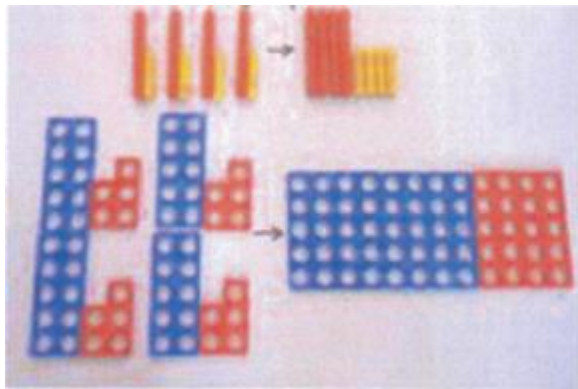
$$\begin{array}{r} 3 \ 9 \ \square \\ - \square \ \square \ 6 \\ \hline \square \ 0 \ 5 \end{array}$$

Key language that should be used: double, times, multiplied by, the product of, groups of, lots of, 'is equal to' 'is the same as'

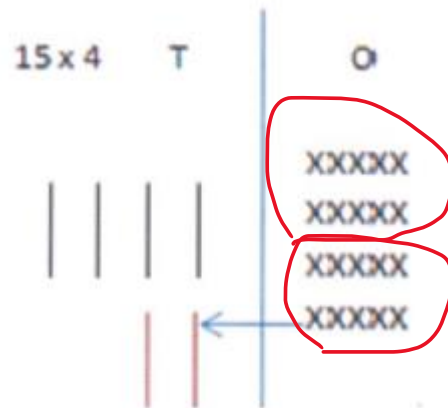
Concrete	Pictorial	Abstract
<p><b>Repeated grouping/ repeated addition</b> (it does not have to be restricted to cubes) 3 x 4 or 3 lots of 4 or 3 groups of 4</p> 	<p>Children to represent the practical resources in a picture e.g.</p> <p style="text-align: center;">XX XX XX XX XX XX</p> <p>Use of Bar Model for a more structured method.</p> 	<p><math>3 \times 4 =</math> <math>4 + 4 + 4 =</math></p>
<p><b>Use number lines to show repeated groups</b> <math>3 \times 4</math></p> 	<p>Represent this pictorially alongside a number line. e.g.</p> 	<p>Abstract Number Line</p> <p><math>3 \times 4 = 12</math></p> 
<p><b>Use Arrays to illustrate commutativity</b> (counters and other objects can also be used)</p> <p><math>2 \times 5 = 5 \times 2</math></p> 	<p>Children to draw the arrays.</p> <p> <math>2 \times 5 = 10</math></p> <p> <math>5 \times 2 = 10</math></p>	<p>Children to be able to use an array to write a range of calculations.</p> <p></p> <p><math>2 \times 5 = 10</math> <math>5 \times 2 = 10</math> <math>5 + 5 = 10</math> <math>2 + 2 + 2 + 2 = 10</math></p>



**Partition to multiply** (use Numicon, Base 10, Cuisenaire rods, unifix etc.)



Children to represent the concrete manipulatives in a picture. e.g. Base 10 can look like this.



6 lots of 10 = 60      15 x 4 = 60

Children to be encouraged to show the steps they have taken.

$$4 \times 15$$

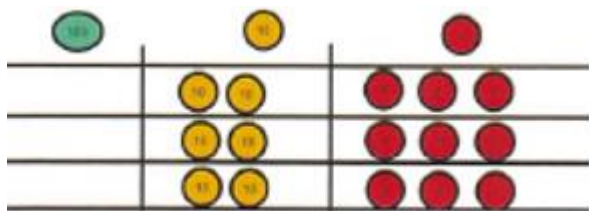
$$\begin{array}{r} 10 \\ 5 \end{array}$$

10 x 4 = 40  
5 x 4 = 20  
40 + 20 = 60

A number line can also be used.

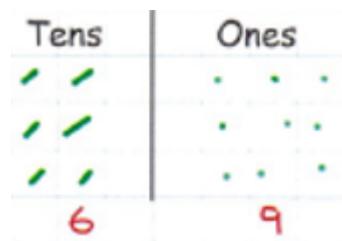
**Formal column method** with place value counters or base 10 (at the first stage- no exchange)

You need to make 23 three times.  
See how many ones and how many tens.



60 + 9

Children to represent the counters in a pictorial way.



Children record what it is they are doing to show understanding.

$$3 \times 23$$

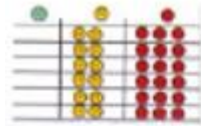
$$\begin{array}{r} 20 \\ 3 \end{array}$$

3 x 20 = 60  
3 x 3 = 9  
60 + 9 = 69

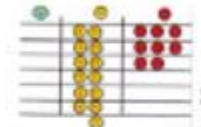
**Formal column method** with place value counters (children need this stage, initially, to understand how the column method works.

$$6 \times 23 =$$

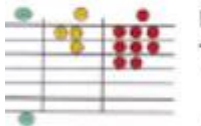
**Step 1:** get 6 lots of 23



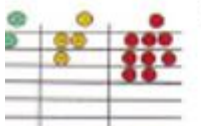
**Step 2:**  $6 \times 3$  is 18. Can I make an exchange? Yes! Ten ones for one ten....



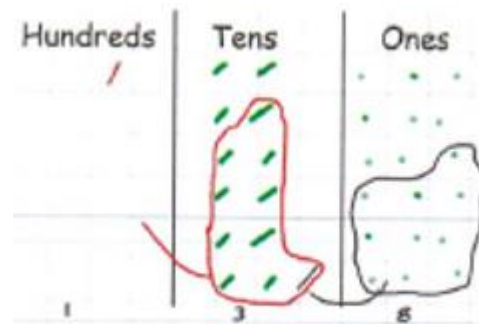
**Step 3:**  $6 \times 2$  tens and my extra ten is 13 tens. Can I make an exchange? Yes! Ten tens for one hundred....



**Step 4-** what do I have in each column?



Children need to represent the counters/ Base 10 pictorially e.g. the image below.



$$6 \times 23$$

$$6 \times 3$$

$$6 \times 20$$

$$120 + 18$$

$$6 \times 23 = 138$$

$\begin{array}{r} \times 6 \\ 20 \\ \hline 318 \end{array}$	$\begin{array}{r} 120 \\ 18^+ \\ \hline 138 \end{array}$
---	--

More examples:  
 $17 \times 3 = 51$

$\begin{array}{r} \times 3 \\ 10 \\ \hline 721 \end{array}$	$\begin{array}{r} 30 \\ 21^+ \\ \hline 51 \end{array}$
---	--

$$28 \times 14 = 392$$

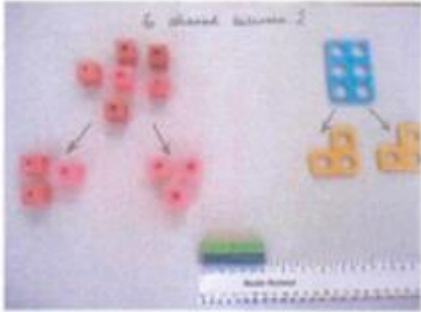
$\begin{array}{r} \times 20 \\ 10 \\ \hline 480 \end{array}$	$\begin{array}{r} 8 \\ 80 \\ \hline 32 \end{array}$	$\begin{array}{r} 200 \\ 80 \\ 80^+ \\ 32 \\ \hline 392 \end{array}$
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## Division

Key language that should be used: share, group, divide, divided by, half, 'is equal to' 'is the same as'

### Concrete

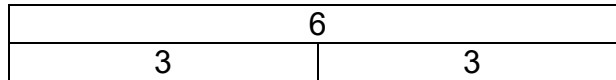
**6 shared between 2** (other concrete objects can also be used e.g. children and hoops, teddy bears, cakes and plates.



### Pictorial



This can be done in a bar so all 4 operations have a similar structure.

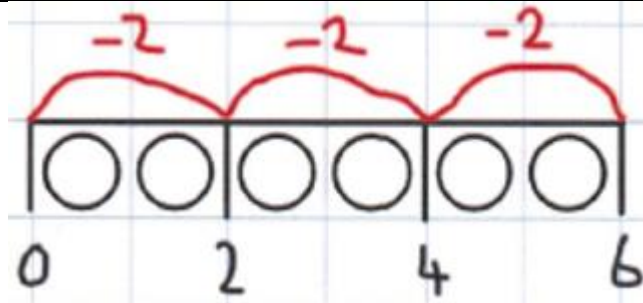
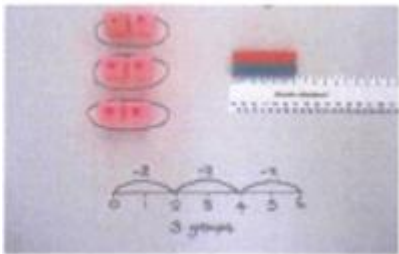


### Abstract

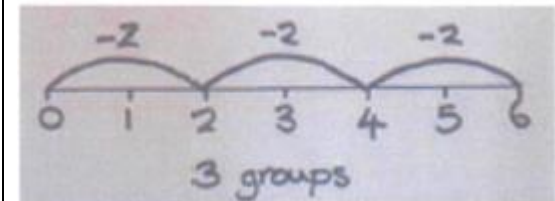
$$6 \div 2 = 3$$

**Understand division as repeated grouping and subtracting.**

$$6 \div 2 = 3$$



Abstract number line

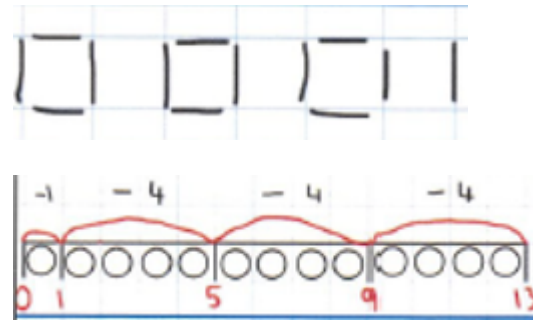


**Division using remainders**

13 divided by 4 = 3 r1

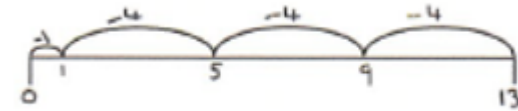


Children to have a chance to represent the resources they use in a pictorial way e.g. see below:



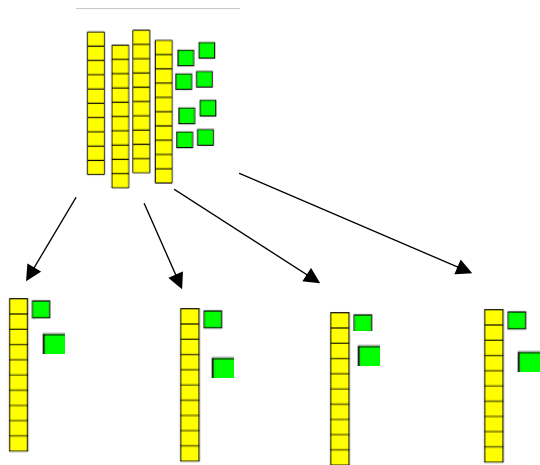
13 divided by 4 = 3r1

Children to count using their times tables facts in their heads.



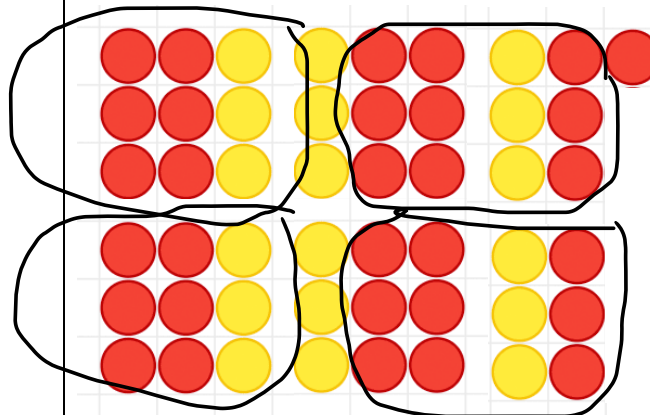
**Sharing using Base 10** (no remainders to start with)

$48 \div 4 = 12$



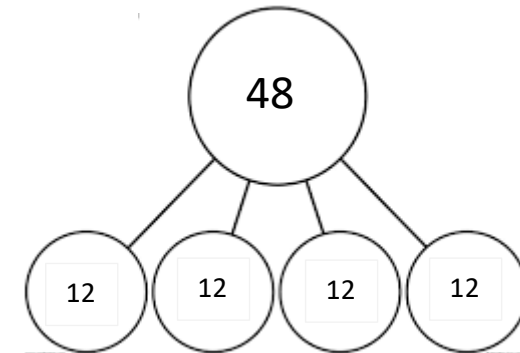
This can also be represented pictorially, till the children no longer need to do it. It can also be done as decimal places if you have remainders.

$49 \div 4 = 12r1$



$48 \div 4 = 12$

48			
12	12	12	12

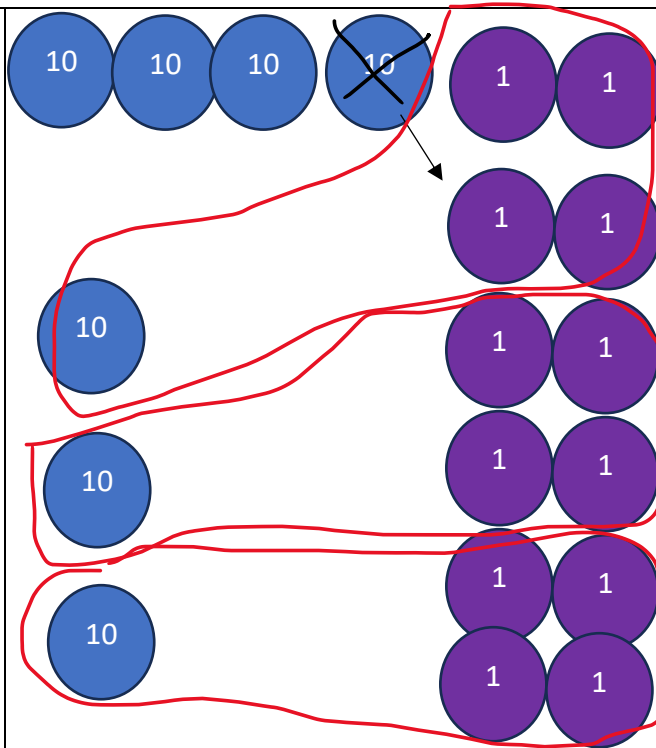


**Sharing using place value counters.**

$$42 \div 3 = 14$$

1. Make the 42
2. Exchange the 4<sup>th</sup> ten and turn into 10 ones.
3. Share the 10 ones into the three groups.

T	O
●	● ● ● ●
●	● ● ● ●
●	● ● ● ●
●	



Children think about what they know. They might partition the numbers.

$$42 \div 3 = 14$$

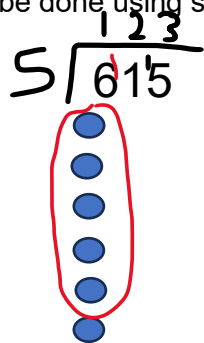
$$42 = 30 + 12$$

$$30 \div 3 = 10$$

$$12 \div 3 = 4$$

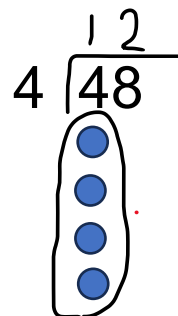
$$10 + 4 = 14$$

**Use of the Bus Stop Method** using grouping and counters. Key language for grouping 'How many groups of X can we make with X' This can be done using sharing.



They children can be represented pictorially until the children no longer need it.

$$48 \div 4 =$$



How many 4s in 4?

How many 4s in 8?

You can even use counters to show this.

$$48 \div 4 =$$

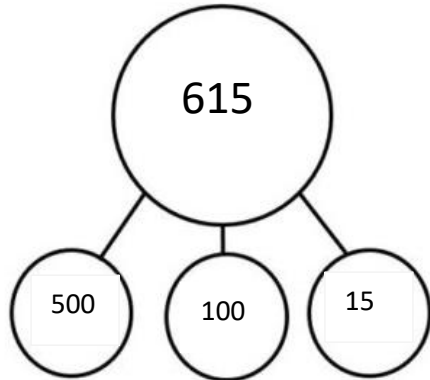
$$4 \overline{)48}$$

How many 4s in 4?

How many 4s in 8?

## Fluency variation, different ways to ask children to solve $615 \div 5$ :

Use the Whole Model below. How can you divide 615 by 5 without using the Bust Stop Method.



How many 5s in 500? **100**

How many 5s in 100? **20**

How many 5s in 15? **3**

Add up  $100+20+3 = 123$

I have £615 and share it equally between 5 bank accounts. How much will be in each bank?

615 pupils need to be put into 5 groups. How many will be in each group?

$$\begin{array}{r} 123 \\ 5 \overline{)615} \end{array}$$

1. How many 5s in 6? **1**
2. Carry the remaining 100 in front of the 1 ten.
3. How many 5s in 11? **2**
4. Carry the remaining 10 over to the 5.
5. How many 5s in 15? **3**

$$615 \div 5 =$$

$$\square = 615 \div 5$$

How many 5s in 615?

What is the calculation?

$$615 \div 5 =$$

How could we solve this?

Partition the number

600 and 10 and 5

If there are 12 lots of 5 in 60 there must be 120 lots of 5 in 600.

There are 2 lots of 5 in 10.

There is 1 lot of 5 in 5.

If you add up the answers...

$$120 + 2 + 1 = 123$$